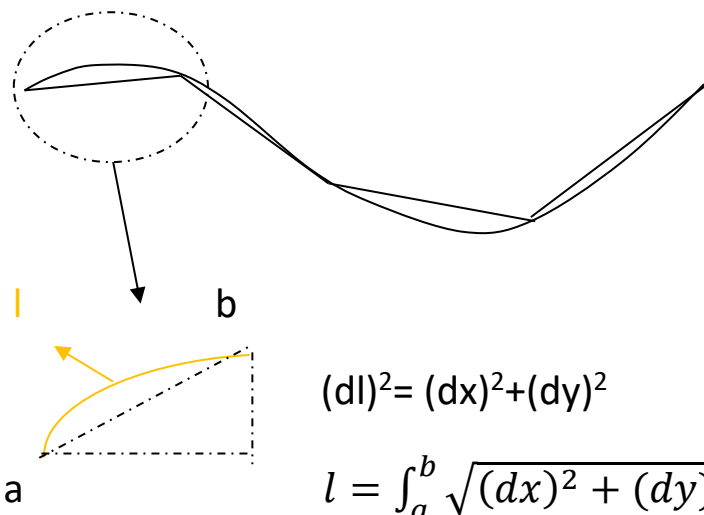


ARCLENGTH:



i sabent la definició de derivada: " $f'(x) = dy/dx$ "

$$l = \int_a^b \sqrt{1 + (f'(x))^2} dx$$

En triangle no rectangle $s = \int_a^b \sqrt{(x'(t))^2 + (y'(t))^2} dt$

$$x(t) = u(t) \quad i \quad y(t) = v(t) \quad s = \int_a^b \sqrt{\left\| \frac{d}{dt} \vec{r}(u(t), v(t)) \right\|^2} dt =$$

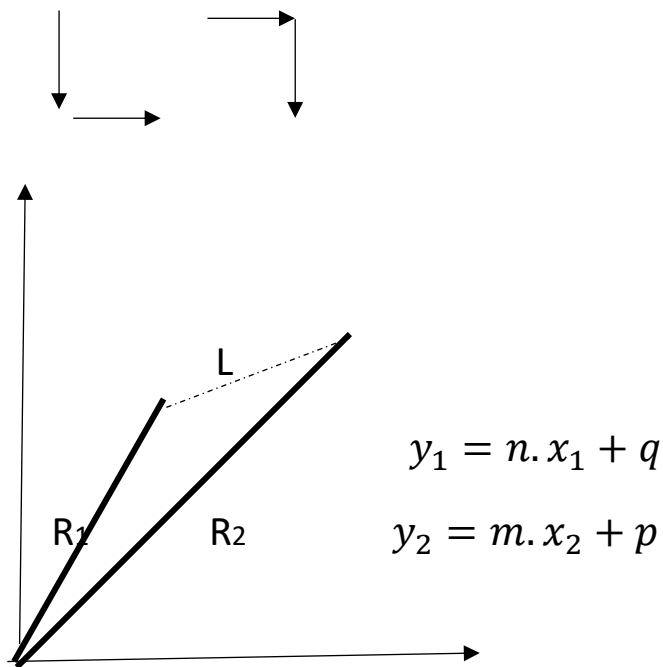
$$= \int_a^b \sqrt{u'(t)^2 \vec{r}_u \vec{r}_u + 2u'(t)v'(t) \vec{r}_u \vec{r}_v + v'(t)^2 \vec{r}_v \vec{r}_v} dt$$

On \vec{r}_u i \vec{r}_v són els respectius vectors unitaris de $u(t)$ i $v(t)$.

$$ds^2 = (du \ dv) \begin{bmatrix} E & F \\ F & G \end{bmatrix} \begin{bmatrix} du \\ dv \end{bmatrix} \quad \text{on } E = \vec{r}_u \vec{r}_u, \quad F = \vec{r}_u \vec{r}_v, \quad G = \vec{r}_v \vec{r}_v$$

i on $\vec{r} = \vec{u} + \vec{v}$ si \vec{u} fos perpendicular a \vec{v} el terme $2u'(t)v'(t)\vec{r}_u\vec{r}_v$ no existiria

Segons Hermite: $g_{12} = g_{21}$



$$\Delta x = \frac{y_2 - p}{m} - \frac{y_1 - q}{n}$$

$$\Delta y = y_2 - y_1$$

Quan hi apareix la variable temps, $n_1 = n + v \cdot t_0$ i $m_1 = m + v \cdot t_0$

O sigui: $n = v_1 \cdot t_n$ i $m = v_2 \cdot t_n$

$$\int dL = \int \sqrt{\left(\frac{y_2 - p}{m_1} - \frac{y_1 - q}{n_1}\right)^2 \cdot g_{11} + 2 \cdot \left(\frac{y_2 - p}{m_1} - \frac{y_1 - q}{n_1}\right) (y_2 - y_1) \cdot g_{12} + (y_2 - y_1)^2 \cdot g_{22}}$$

Si multipliquem i dividim per dt, on $dt = t_n - t_0$

$$\int \sqrt{\left(\frac{y_2 - p}{m_1} - \frac{y_1 - q}{n_1}\right)^2 \cdot g_{11} + 2 \cdot \left(\frac{y_2 - p}{m_1} - \frac{y_1 - q}{n_1}\right) (y_2 - y_1) \cdot g_{12} + (y_2 - y_1)^2 \cdot g_{22}}$$

$$\int \sqrt{\left(\frac{y_2 - p - y_1 - q}{m_1 n_1 dt^2}\right)^2 \cdot g_{11} + 2 \cdot \left(\frac{y_2 - p - y_1 - q}{m_1 n_1 dt^2}\right) (y_2 - y_1) \cdot g_{12} + \left(\frac{y_2 - y_1}{dt^2}\right)^2 \cdot g_{22}} \cdot dt$$

$$\int dL = \int \sqrt{\left(\frac{[y_2 n_1 - p n_1 - y_1 m_1 + q m_1]}{dt^2 m_1 n_1}\right)^2 \cdot g_{11} + 2 \cdot \left(\frac{[y_2 n_1 - p n_1 - y_1 m_1 + q m_1]}{dt^2 m_1 n_1}\right) \cdot (y_2 - y_1) \cdot g_{12} + \left(\frac{y_2 - y_1}{dt^2}\right)^2 g_{22}} dt$$

I usant les condicions inicials: valors de y_1 i y_2 i t_0 i t_n podrem deduir L, suposant que t és la variable!!.