

LAGRANGIAN:

transformation : represents a kind of **recalibration** or transformation of one degree of freedom of the internal system that does not alter any physical property . It is like a kind of theory of relativity where we take as a reference a coordinate axis (or degrees of freedom) randomly without to influence the “ scalar ” values that are they fight .

We can also talk about **hyperspace** : space in 3 or more dimensions .

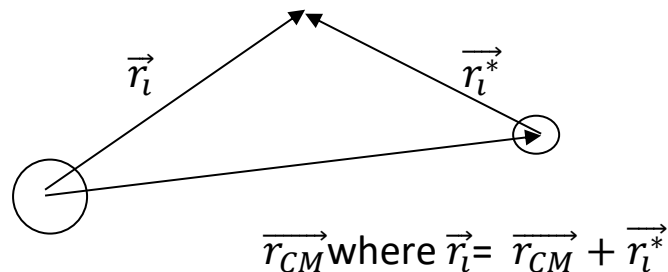
When it comes to **bosons** and **fermions** : we meet first present in interactions between particles subatomic (disintegration) , while the according to they have to do with with matter exchanges .

At every energy level constitutes a dimension?

About Planck	{	- Planck length: the basic and first λ
		(with respect to photons): $\lambda \propto 1/\nu$, where ν =frequency
		-quantum : h: the elementary quantum of action.

Sometimes we can conceive others dimensions as “superpositions” of volumes or figures that converge with each other others from the 3rd^{era} dimension .

and



with speeds and energies is similar

We can to study the **Lagrangian** :

$$\frac{\partial L}{\partial q_i} = \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_i} \right) \quad \text{where } L = f(x, v, t) = f(x, \dot{x}, t)$$

gives , therefore , a scalar.

$$\frac{d}{dt} \left(\frac{\partial L(p_i(t), \dot{p}_i(t), t)}{\partial \dot{p}_i} \right) - \frac{\partial L(p_i(t), \dot{p}_i(t), t)}{\partial p_i} = 0$$

p_i position, $\dot{p}_i$ speed

$$\text{We deduce that } \dot{p}_i = \frac{dp_i}{dt} \quad \text{and} \quad \ddot{p}_i = \frac{d\dot{p}_i}{dt}$$

$$F. \delta r = m. \ddot{r}. \delta r$$

We know that the Lagrangian = L= TV= Ekinetic -Epotential

$$\text{Then we understand that: Work} = \sum_i^n \left[\frac{\partial}{\partial t} \left(\frac{\partial(T-V)}{\partial \dot{p}_i} \right) - \left(\frac{\partial(T-V)}{\partial p_i} \right) \right] \delta p_i$$

which can be non-conservative forces : work $\neq 0$

Let's check it out :

$$\frac{\partial}{\partial t} \left(\frac{\partial T}{\partial \dot{p}_i} \right) = \frac{\partial}{\partial t} \left(\frac{\frac{1}{2} m \cdot \partial(\dot{p}_i^2)}{\partial \dot{p}_i} \right) = \frac{\partial}{\partial t} \left(\frac{1}{2} \cdot m \cdot \frac{2 \dot{p}_i \cdot \partial \dot{p}_i}{\partial \dot{p}_i} \right) = \frac{\partial}{\partial t} (m \cdot \dot{p}_i) = m \cdot \ddot{p}_i$$

$$\frac{\partial}{\partial t} \left(\frac{\partial V}{\partial \dot{p}_i} \right) = \frac{\partial}{\partial t} \left(\frac{F \cdot \partial p_i}{\partial \dot{p}_i} \right) = F \cdot \left(\frac{\ddot{p}_i \cdot \partial \dot{p}_i - \partial \dot{p}_i \cdot \ddot{p}_i}{\partial \dot{p}_i^2} \right) = 0$$

$$\frac{\partial(T)}{\partial p_i} = \frac{\frac{1}{2} m \cdot \partial(\dot{p}_i^2)}{\dot{p}_i \cdot dt} = \frac{1}{2} \cdot m \cdot \frac{2 \cdot \dot{p}_i \cdot \partial \dot{p}_i}{\dot{p}_i \cdot dt} = m \cdot \frac{\partial \dot{p}_i}{dt} = m \cdot \ddot{p}_i$$

$$\frac{\partial(V)}{\partial p_i} = F \cdot \frac{\partial p_i}{\partial p_i} = F = m \cdot \ddot{p}_i$$

All this has another reading: the angular momentum is $\vec{L} = \vec{r} \times \vec{p}$

where $\vec{L}(p_i, \dot{p}_i)$.

If we derive it with respect to time $\frac{\partial \vec{L}}{\partial t} = \vec{r} \times \frac{\partial \vec{p}}{\partial t} + \frac{\partial \vec{r}}{\partial t} \times \vec{p} = \vec{r} \times \vec{F}$ since $\frac{\partial \vec{r}}{\partial t} = \vec{v}$ and $\vec{p} = m \vec{v}$ they are parallel, then its vector product is =0.

If $\vec{L}$ is constant with respect to time, $\frac{\partial \vec{L}}{\partial t} = 0$

The **Lagrangian** is defined as the remainder between E_c and E_p : $L = T - V$

$$U(r) = V(q) = - \int F dr \quad V = U/q = - \int F dr \quad F(r) = \sum_{i,j} K \cdot \frac{q_i q_j}{r_{ij}^2}$$

$$\partial U(r) = \sum_{i,j} K \cdot \frac{q_j \cdot q_i}{dr_{ij}} = -F \cdot dr$$

$$V = \sum_{i,j} K \cdot \frac{q_i q_j}{r_{ij}}$$